External assessment 2024

Multiple choice question book

# **Mathematical Methods**

Paper 1 — Technology-free

# **General instruction**

• Work in this book will not be marked.





# Section 1

## Instruction

• Respond to these questions in the question and response book.

# **QUESTION 1**

Determine  $\int x^4 dx$ 

(A)  $4x^{3} + c$ (B)  $5x^{5} + c$ (C)  $\frac{1}{3}x^{3} + c$ (D)  $\frac{1}{5}x^{5} + c$ 

# **QUESTION 2**

Determine  $\frac{dy}{dx}$  for the function  $y = e^{\sin(x)}$ 

- (A)  $\cos(x) e^{\sin(x)}$
- (B)  $\sin(x) e^{\cos(x)}$
- (C)  $e^{\sin(x)}$
- (D)  $e^{\cos(x)}$

#### **QUESTION 3**

A sample of size *n* can be used to obtain a sample proportion  $\hat{p}$ .

An approximate margin of error for the population proportion can be obtained using the formula

$$E = z \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

If the level of confidence is increased from 95% to 99%, then

- (A) the associated *z*-value would decrease, so *E* would increase.
- (B) the associated *z*-value would increase, so *E* would increase.
- (C) the associated *z*-value would decrease, so *E* would decrease.
- (D) the associated *z*-value would increase, so *E* would decrease.

## **QUESTION 4**

Simplify  $y = 2\ln(e^x)$ 

- (A) y = 2x
- (B)  $y = 2^x$

(C) 
$$y = \frac{2}{x}$$

(D)  $y = x^2$ 

#### **QUESTION 5**

Determine  $\int_{a}^{b} 2\cos(x) dx$ , where  $a = \frac{\pi}{3}$  and  $b = \frac{\pi}{2}$ 

(A) 
$$1 - \frac{\sqrt{3}}{2}$$
  
(B)  $\frac{\sqrt{3}}{2} - 1$   
(C)  $2 - \sqrt{3}$   
(D)  $\sqrt{3} - 2$ 

## **QUESTION 6**

Differentiate  $y = \ln(x) \cos(x)$  with respect to x.

(A)  $\frac{\cos(x)}{x}$ (B)  $-\frac{\sin(x)}{x}$ (C)  $\frac{\cos(x)}{x} + \ln(x)\sin(x)$ (D)  $\frac{\cos(x)}{x} - \ln(x)\sin(x)$ 

## **QUESTION 7**

Twenty families are selected to participate in a lifestyle study related to family size. The number of children in these families is uniformly distributed as shown.



A random sample of five families is chosen from this group, without replacement. A possible mean number of children in the sample is

- (A) 5.0
- (B) 2.0
- (C) 1.0
- (D) 0.0

# **QUESTION 8**

The graph of f(x) is shown.



 $\frac{1}{3}$  x

Identify the graph of the second derivative f''(x).





# **QUESTION 9**

At a certain location, the temperature (°C) can be modelled by the function  $T = 5\sin\left(\frac{\pi}{12}x\right) + 23$ , where x is the number of hours after sunrise.

Determine the rate of change of temperature (°C/hour) when x = 4

(A)	$5\pi$
	48

- (B)  $\frac{5\pi}{24}$
- (C)  $\frac{5\pi\sqrt{3}}{24}$
- (D)  $\frac{5\pi\sqrt{3}}{6}$

### **QUESTION 10**

Given that  $\log_{10} 6 = 0.778$ , determine the value of  $\log_{10} 600$ 

- (A) 77.800
- (B) 10.778
- (C) 2.778
- (D) 1.556

# THIS PAGE IS INTENTIONALLY BLANK

Ĵ

© State of Queensland (QCAA) 2024 Licence: https://creativecommons.org/licenses/by/4.0 | Copyright notice: www.qcaa.qld.edu.au/copyright — lists the full terms and conditions, which specify certain exceptions to the licence. | Attribution: © State of Queensland (QCAA) 2024