# General Mathematics marking guide and response

External assessment 2024

Paper 1: 57 marks

Paper 2: 38 marks

#### Assessment objectives

This assessment instrument is used to determine student achievement in the following objectives:

- 1. select, recall and use facts, rules, definitions and procedures drawn from Units 3 and 4
- 2. comprehend mathematical concepts and techniques drawn from Units 3 and 4
- 3. communicate using mathematical, statistical and everyday language and conventions
- 4. evaluate the reasonableness of solutions
- 5. justify procedures and decisions by explaining mathematical reasoning
- 6. solve problems by applying mathematical concepts and techniques drawn from Units 3 and 4.





## Purpose

This marking guide:

- provides a tool for calibrating external assessment markers to ensure reliability of results
- indicates the correlation, for each question, between mark allocation and qualities at each level of the mark range
- informs schools and students about how marks are matched to qualities in student responses.

The sample response:

- demonstrates the qualities of a high-level response
- has been annotated using the marking guide.

## Mark allocation

Where a response does not meet any of the descriptors for a question or a criterion, a mark of '0' will be recorded.

Where no response to a question has been made, a mark of 'N' will be recorded.

Allow FT mark/s — refers to 'follow through', where an error in the prior section of working is used later in the response, a mark (or marks) for the rest of the response can be awarded so long as it still demonstrates the correct conceptual understanding or skill in the rest of the response.

This mark may be implied by subsequent working — the full mathematical reasoning and/or working, as outlined in the sample response and associated mark, is not explicitly stated in the student response, but by virtue of subsequent working there is sufficient evidence to award the mark/s.

## Marking guide

## Multiple choice

Question	Response
1	В
2	D
3	В
4	D
5	С
6	А
7	С
8	С
9	D
10	С
11	В
12	А
13	А
14	С
15	A

## Paper 1: Short response

Q	Sample response				The response:		
16a)	$t_2 = t_1 + 8$ = 25 + 8 = 33 The second row of	the the	atre ha	s 33 se	• correctly determines the number of seats in the second row [1 mark]		
16b)	$t_3 = t_2 + 8$ $t_3 = 33 + 8$ = 41	$t_4 = t_3 + t_3 + t_4 = 41 + t_4 = 49$	8 • 8				
	Row Number of seats	1 25	2 33	3 41	4 49		• correctly completes the table to display the first four terms <b>[1 mark]</b>
	Total number of se = $25 + 33 + 41 + 4$ = 148	ats in fi 9	rst fou	r rows	heatre	• calculates total number of seats in first four rows [1 mark]	
17a)	A planar graph can each other.	ı be drav	wn so t	hat no	edges o	cross	• correctly defines a planar graph [1 mark]
17b)	5 faces						• correctly states the number of faces [1 mark]

Q	Sample response	The response:
17c)	<i>v</i> = 6	• correctly identifies the number of vertices
	<i>e</i> = 9	and edges for the graph [1 mark]
	v+f-e	
	= 6 + 5 - 9	
	= 2	• shows Euler's formula works for the graph [1 mark]
18	Using compound interest rule	
	P = 3000	
	$i = \frac{0.042}{12} = 0.0035$	
	$n = 18 \times 12 = 216$	• correctly determines the <i>i</i> and <i>n</i> values [1 mark]
	$A = P(1+i)^n$	
	$=3000 \times (1 + 0.0035)^{216}$	• substitutes into appropriate rule [1 mark]
	<i>A</i> = <b>6380.79</b>	• determines value of investment [1 mark]
	I = A - P	
	= 6380.79 - 3000	
	= 3380.79	• determines amount of interest earned
	The amount of interest earned is \$3380.79.	[1 mark]

Q	Sample response	The response:
19a)	25 20 15 15 15 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	<ul> <li>correctly identifies the explanatory and response variables [1 mark]</li> <li>accurately plots points [1 mark]</li> <li>formats scatterplot with appropriate scaling and labelling of axes [1 mark]</li> </ul>
19b)	The form of the relationship is <b>linear</b> .	• states form as linear [1 mark]
20a)	Pearson's correlation coefficient is <b>0.986</b> . So, it is a <b>strong</b> association.	<ul> <li>correctly identifies the value of Pearson's correlation coefficient [1 mark]</li> <li>correctly describes the strength as strong [1 mark]</li> </ul>
20b)	A confounding variable is another variable that has a similar effect on the response variable.	• correctly defines confounding variable [1 mark]
20c)	Air temperature, $x$ , and number of vehicles, $y$ , are both lower at earlier and later times of day when train user vehicles are arriving and leaving the train station; and are both higher in the middle of the day when train users are at work.	<ul> <li>correctly explains why <i>t</i> could be a confounding variable [1 mark]</li> </ul>
21a)	Quarterly interest rate, $i = \frac{5.2}{100 \times 4}$ = 0.013	• correctly determines the quarterly interest rate [1 mark]

Q	Sample response	The response:
21b)	$A = \frac{M}{i}$	
	$A = \frac{975}{0.013}$	• substitutes into appropriate rule [1 mark]
	$A = 75\ 000$ The value of the perpetuity is \$75 000.	• calculates value of perpetuity [1 mark]
22a)	Monthly rate $=\frac{8.4}{100 \times 12} = 0.007$	• correctly calculates the monthly interest rate [1 mark]
	$A_{n+1} = rA_n - R$	
	$A_{n+1} = 1.007A_n - 250$	• determines recurrence relation [1 mark]
22b)	$A_0 = 15\ 000$	
	$A_1 = 1.007 \times 15\ 000 - 250 = 14\ 855$	• determines lean halance after two months
	$A_2 = 1.007 \times 14855 - 250 = 14708.99$	[1 mark]
	Loan balance after two months is \$14 /08.99	

Q	Sample response	The response:
22c)	<b>Method 1</b> Reduction in loan balance = 15 000 - 14 708.99 = \$291.01	• determines reduction in loan balance in first two months <b>[1 mark]</b>
	Total repayments = $2 \times 250 = $ <b>\$500</b>	• determines total repayments in first two months [1 mark]
	Total amount of interest paid in first two months = total repayments – reduction in loan balance = $2 \times 250 - 291.01$ = \$208.99	• determines total amount of interest paid
	φ_0000	in the first two months [1 mark]
	Method 2	
	Interest paid in month $1 = 0.007 \times 15\ 000 = 105$	<ul> <li>determines interest paid in first month [1 mark]</li> </ul>
	Interest paid in month $2 = 0.007 \times 14855 = 103.99$	• determines interest paid in second month [1 mark]
	Total amount of interest paid in first two months	
	= 105 + 103.99	
	= \$208.99	• determines total amount of interest paid in the first two months <b>[1 mark]</b>

Q	Sample response	The response:
23a)	Minimum spanning tree: Q 235 R 230 345 230 $345200$ S $210$ T $360$ U 440 $280$ $260$ $320$ W	<ul> <li>correctly draws a spanning tree on the diagram [1 mark]</li> <li>correctly draws the minimum spanning tree on the diagram [1 mark]</li> </ul>
23b)	Minimum total pipeline length = 235 + 230 + 200 + 210 + 280 + 260 + 320 = 1735 km 1735 < 2000, so 2000 km of pipeline is sufficient.	<ul> <li>determines minimum total pipeline length [1 mark]</li> <li>provides appropriate statement of reasonableness linked to prior working [1 mark]</li> </ul>

Q	Sar	nple i	respo	onse			The response:	
24a)	A B C D E F	A 0 0 0 0 1 1	B 0 1 0 1 0	C 0 1 0 1 1 1 0	D 0 1 0 1 1 0	E 1 1 1 1 0 1	F 1 0 0 1 1 0	<ul> <li>correctly completes entries for one row or one column in a 6 × 6 matrix with same horizontal and vertical labels [1 mark]</li> <li>correctly completes adjacency matrix [1 mark]</li> </ul>
24b)	Sin	nple, o	conn	ected			• correctly identifies simple and connected only [1 mark]	
24c)	Stu stud	dents dent (	<b>B, E</b> C.	<b>)</b> and	E stu	ıdy a	ubject to • correctly identifies B, D and E only [1 mark]	
24d)	F●		E	A		•C	• correctly draws and labels a connected subgraph that contains student E and has three edges and no cycles [1 mark]	

Q	Sample res	sponse	)		The response:		
25a)	2022 mean 2023 mean	ı rainfa ı rainfa	11 = (410 + 11) = (390 + 11)	30 + 205 + 20 + 150 +	- 1135)/4 = 4 - 1100)/4 = 4	145 115	• correctly calculates the 2022 mean rainfall and 2023 mean rainfall [1 mark]
			2022		2023		• calculates seasonal ratios for 2022
	Autumn	410/4	45 = 0.921	3 390/4	15 = <b>0.9398</b>		and 2023 [1 mark]
	Winter	30/44	15 = 0.0674	20/41	5 = 0.0482		
	Spring	205/4	45 = 0.460	7 150/4	15 = 0.3614		
	Summer	1135	/445 = 2.55	06 1100/	415 = 2.650	6	
	Autumn Winter Spring	(0.92 (0.06 (0.46	$5eas \\ 13 + 0.9398 \\ 74 + 0.0482 \\ 07 + 0.3614 \\ 07 + 00$	(3)/2 = 0.93 (2)/2 = 0.05 (4)/2 = 0.41	06 78 11	-	season [1 mark]
	Summer	(2.55	06 + 2.6506	6)/2 = 2.60	06		
25b)	Deseasona	AutumnWinterSpringnalised130/0.92145/1.02155/1.12all= 141.30= 142.16= 138.39				Summer 132/0.94 = 140.43	• correctly calculates the deseasonalised rainfall for each season [1 mark]
	Winter has	the high	ghest seasor	nally adjus	ted rainfall.	• identifies season with highest seasonally adjusted rainfall	

### Paper 2: Short response

Q	Sample resp	onse			The response:
1		Year 11	Year 12	Total	• correctly calculates the frequencies for total Year 11 students and total Year 12
	Musician	32 - 8 =	half of	24 + 14	students [1 mark]
		24	28 = 14	= 38	• calculates frequencies for dancers in Year 11 and dancers in Year 12 [1 mark]
	Dancer	quarter of $32 = \frac{8}{8}$	half of 28 = 14	8 + 14 = <b>22</b>	• calculates frequencies for musicians in Year 11 and musicians in Year 12 [1 mark]
	Total	32	28	60	• calculates frequencies for total musicians and total dancers [1 mark]
	Percentage o $\frac{38}{60} \times 100\% =$	f students w 63.3%	'ho are mu	• calculates percentage of students who are musicians [1 mark]	

Q	Sample response	The response:
2	R $25$ $K$ $20$ $16$ $14$ $18$ $N$ $R$	<ul> <li>correctly constructs a graph showing all 5 labelled vertices and all 6 edges [1 mark]</li> <li>correctly shows weights on all 6 edges [1 mark]</li> </ul>
	Hamiltonian cycle beginning at Waiben: WGPKNW	<ul> <li>identifies a Hamiltonian cycle beginning at Waiben [1 mark]</li> </ul>
	= 14 + 16 + 25 + 20 + 18 $= 93  min$	• determines total travel time [1 mark]

Q	Sample response	The response:
3	slope, $b = -0.227$ vertical axis intercept, $a = 16.7$	• correctly determines the values for the slope and vertical axis intercept [1 mark]
	y = a + bx	
	y = 16.7 - 0.227x	• determines least-squares line equation [1 mark]
	Let $x = 43$	
	y = 16.7 + -0.227(43)	<ul> <li>substitutes latitude into least-squares line equation</li> <li>[1 mark]</li> </ul>
	<i>y</i> = 6.9	
	The predicted ultraviolet index is 7.	• predicts UV index [1 mark]
	The notification is reasonable because an ultraviolet index of 7 corresponds to high.	• provides appropriate statement of reasonableness linked to prior working <b>[1 mark]</b>





Q	Sample response	The response:
	Number of lines needed to cover all zeros = number of tasks $(3 = 3)$ , so allocate planes.	
	For minimum distance, the plane allocation is airbase A to site Q, airbase B to site P and airbase C to site R.	• identifies optimal allocation for each plane [1 mark]
	Minimum total distance flown = $600 + 445 + 770$ = 1815 km	• determines minimum total distance flown [1 mark]

Q	Sample response	The response:
5	Method 2 Calculate x (distance from A to P): Angular distance = $28^{\circ} - 20^{\circ} = 8^{\circ}$ $D = 111.2 \times 8^{\circ} \approx 890$ km Calculate y (distance from A to R): Angular distance = $147^{\circ} - 136^{\circ} = 11^{\circ}$ $D = 111.2 \times acc 20^{\circ} \times 11^{\circ} \approx 1140$ km	<ul> <li>correctly calculates distance x in kilometres [1 mark]</li> <li>correctly calculates distance y in kilometres</li> </ul>
	$D = 111.2 \times \cos 20^{\circ} \times 11^{\circ} \approx 1149 \text{ km}$ $P  Q  R$ $A  890  600  1149$ $B  445  485  340$ $C  980  1170  770$ $column$ $-445  -485  -340$ $reduction$ $row reduction$	[1 mark]
	$\begin{bmatrix} 445 & 115 & 809 \\ 0 & 0 & 0 \\ 535 & 685 & 430 \end{bmatrix} \begin{array}{c} -115 \\ 0 \\ -430 \end{bmatrix}$	• reduces each column [1 mark]
	$\begin{bmatrix} 330 & 0 & 694 \\ \hline 0 & 0 & 0 \\ \hline 105 & 255 & 0 \end{bmatrix}$	• reduces each row [1 mark]

Q	Sample response	The response:
	Number of lines needed to cover all zeros = number of tasks $(3 = 3)$ , so allocate planes.	
	For minimum distance, the plane allocation is airbase A to site Q, airbase B to site P and airbase C to site R.	<ul> <li>identifies optimal allocation for each plane</li> <li>[1 mark]</li> </ul>
	Minimum total distance flown = $600 + 445 + 770$ = 1815 km	• determines minimum total distance flown [1 mark]

Q	Sample response			The response:
5	Method 3 Calculate x (distance from Angular distance = $28^{\circ}$ - $D = 111.2 \times 8^{\circ} \approx 890$ km	m A to P): - $20^\circ = 8^\circ$		• correctly calculates distance <i>x</i> in kilometres <b>[1 mark]</b>
	Calculate y (distance from Angular distance = $147^{\circ}$ $D = 111.2 \times \cos 20^{\circ} \times 11^{\circ}$	m A to R): −136° =11° ° ≈ <b>1149</b> km		• correctly calculates distance y in kilometres [1 mark]
	Possible Allocation		Total distance (km)	
	A to P, B to Q, C to R	890 + 485 + 770	2145	
	A to P, B to R, C to Q A to Q, B to P, C to R A to Q, B to R, C to P	$\frac{890 + 340 + 1170}{600 + 445 + 770}$ $\frac{600 + 340 + 980}{600 + 340 + 980}$	2400 1815 1920	• correctly identifies all six possible allocations [1 mark]
	A to R, B to P, C to Q	1149 + 445 + 1170	2764	• determines total distance for all six
	A to R, B to Q, C to P	1149 + 485 + 980	2614	possible allocations [1 mark]
	For minimum distance, t to site Q, airbase B to sit	he plane allocation is e P and airbase C to s	airbase A site R.	• identifies optimal allocation for each plane [1 mark]
	Minimum total distance = 1815 km	flown = 600 + 445 +	770	• determines minimum total distance flown [1 mark]

Q	Sample response	The response:
6	Daily cost for a person in 2021 ( $n = 1$ ). $m_1 = c = \$60$ $a_1 = 2c = \$120$	• correctly determines values for <i>m</i> <sub>1</sub> and <i>a</i> <sub>1</sub> [1 mark]
	In 2025, <i>n</i> = 5	• correctly determines $n = 5$ [1 mark]
	Daily cost for a person in 2025 for meals: $m_n = m_1 + 3(n-1)$ $m_5 = 60 + 3(5-1)$ = \$72	• uses arithmetric model to determine daily cost for a person in 2025 for meals ( <i>m</i> <sub>5</sub> ) [1 mark]
	Daily cost for a person in 2025 for accommodation: $a_n = a_1 \times 1.1^{(n-1)}$ $a_n = 120 \times 1.1^{(5-1)}$	
	= \$175.69	• uses geometric model to determine daily cost for a person in 2025 for accommodation ( <i>a</i> <sub>5</sub> ) <b>[1 mark]</b>

Q	Sample response	The response:
	Total cost for a person in 2025 for 7 days = $72 \times 7 + 175.69 \times 7$ = \$1733.83	• calculates total cost for a person in 2025 for 7 days <b>[1 mark]</b>
	1500 < 1733.83 < 2000 ∴ The estimate is reasonable as \$1733.83 is between \$1500 and \$2000.	• provides appropriate statement of reasonableness linked to prior working [1 mark]

Q	Sample response	The response:
7	Total flight distance from Sydney to Los Angeles = $4828 + 7242 = 12\ 070\ \text{km}$ Time difference between Sydney (UTC +10) and Los Angeles (UTC -8) = $+10 - (-8) = 18\ \text{hours}$ $\therefore$ Sydney is 18 hours ahead of Los Angeles. Local time and day in Sydney when flight arrives in Los Angeles = $6:50\ \text{pm}\ \text{Tuesday} + 18\ \text{h}$ = $12:50\ \text{pm}\ \text{Wednesday}$	<ul> <li>correctly calculates the total flight distance and the absolute time difference between locations [1 mark]</li> <li>applies relative time difference to Los Angeles arrival time (or Sydney departure time) to determine local time and day in other location [1 mark]</li> </ul>
	Total flight duration from Sydney to Los Angeles = 12:50 pm Wednesday – 9:50 pm Tuesday = 15 hours Proportion of total flight distance when 4828 km travelled $= \frac{4828}{12070} \times 100$ $= 40\%$ Flight duration when 4828 km travelled = 40% of 15 h	• calculates total flight duration <b>[1 mark]</b> • shows use of appropriate method to determine flight duration <b>[1 mark]</b>

Q	Sample response	The response:
	= 6 hours	• determines flight duration when 4828 km travelled [1 mark]
	Local time and day in Sydney when 4828 km travelled = 9:50 pm Tuesday + 6 h = 3:50 am Wednesday	• determines local time and day in Sydney when 4828 km travelled [1 mark]
		• shows logical organisation, communicating key steps [1 mark]

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